

# Statistical methods for cost-effectiveness analysis: a personal history

Andrew Briggs

Professor of Health Economics



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The last 25 years have seen a large increase in the contribution that health economic analysis has made in national and international decisions about health care provision. Andy Briggs has been working at the interface between medical statistics and health economics throughout this period. In this talk he gives a personal history of that journey with an emphasis on how statistical thinking has improved the methods of health economic evaluation over that period. Looking to the future, there remains much potential for statistical methods to continue to improve the way in which we evaluate the cost-effectiveness of health care interventions and to improve health care decision making as a result.

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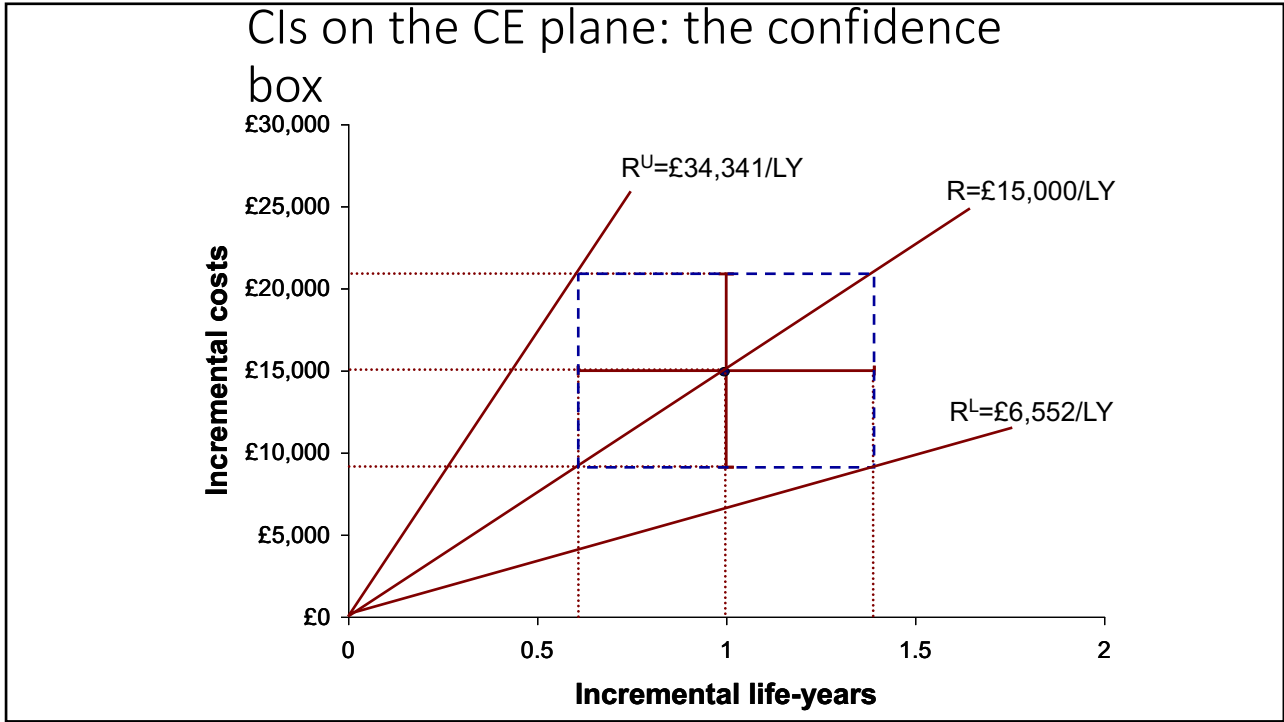
## Statistical methods for cost-effectiveness analysis: a personal history

- Representing uncertainty in cost-effectiveness analysis
- Clinical trials versus decision models: a false dichotomy?
- Statistical decision theory
- Survival analysis
- Comparative effectiveness and the rise of Network Meta Analysis

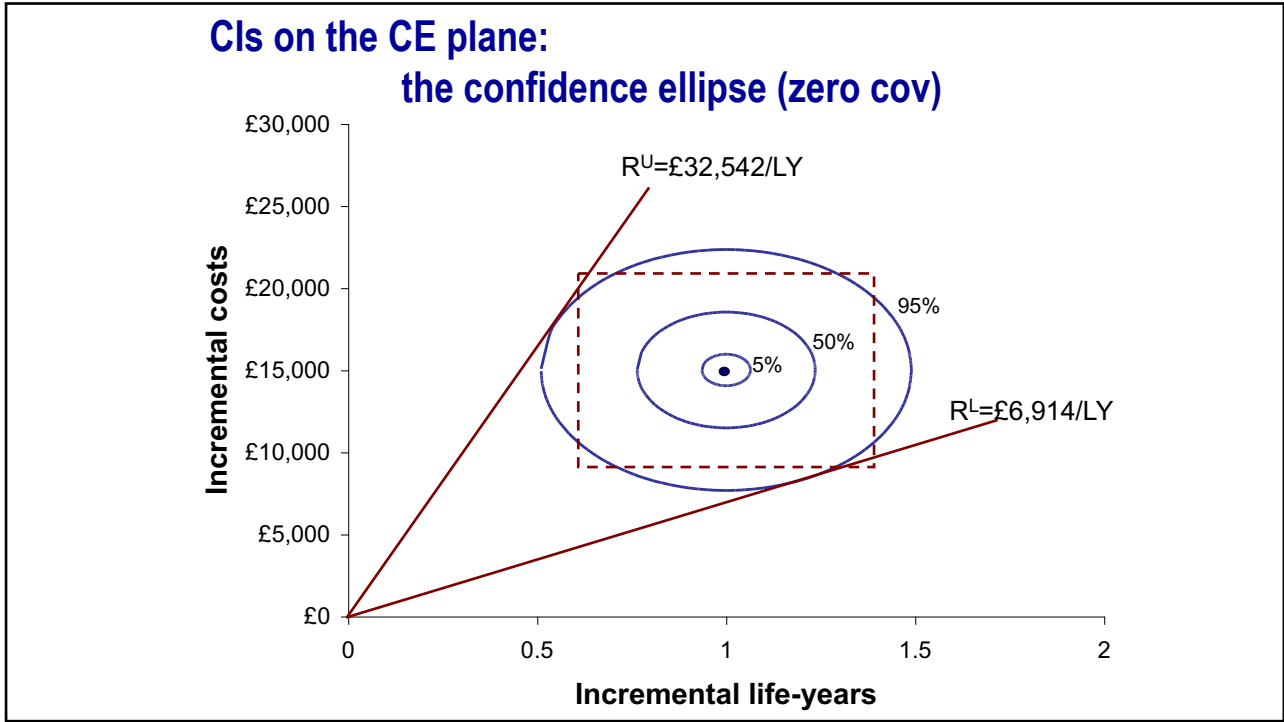
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## Representing uncertainty in CEA

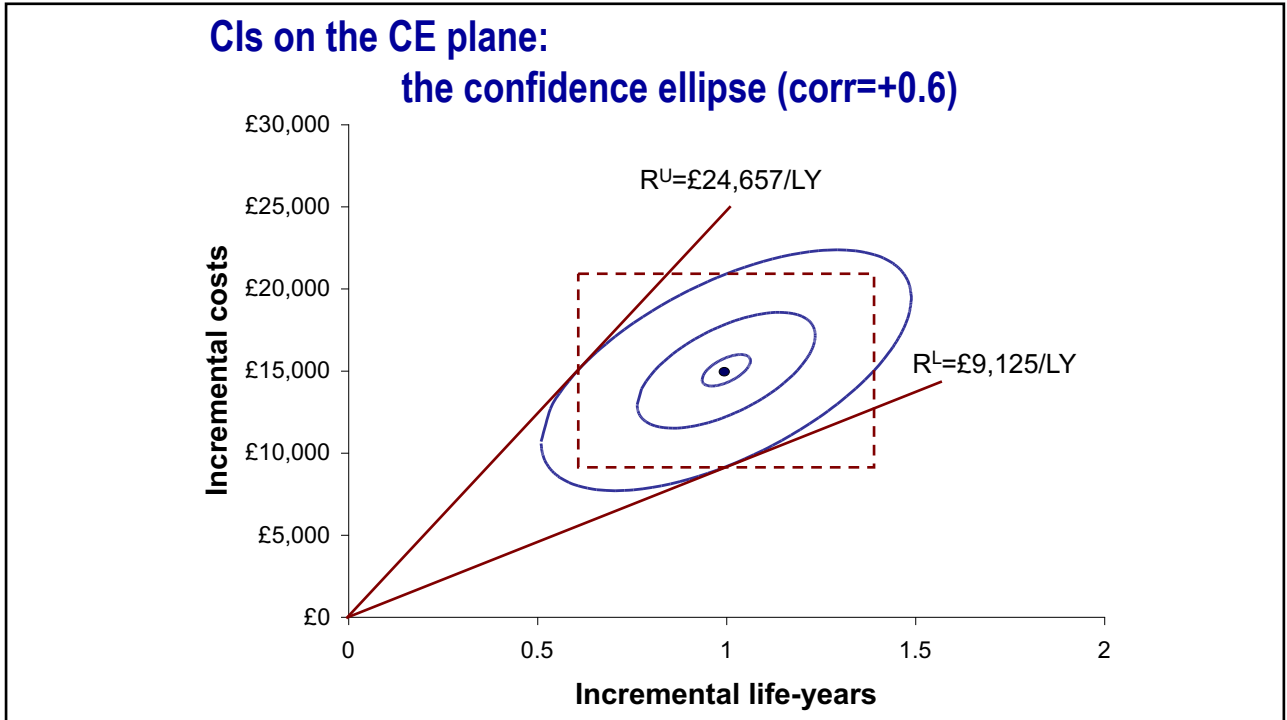
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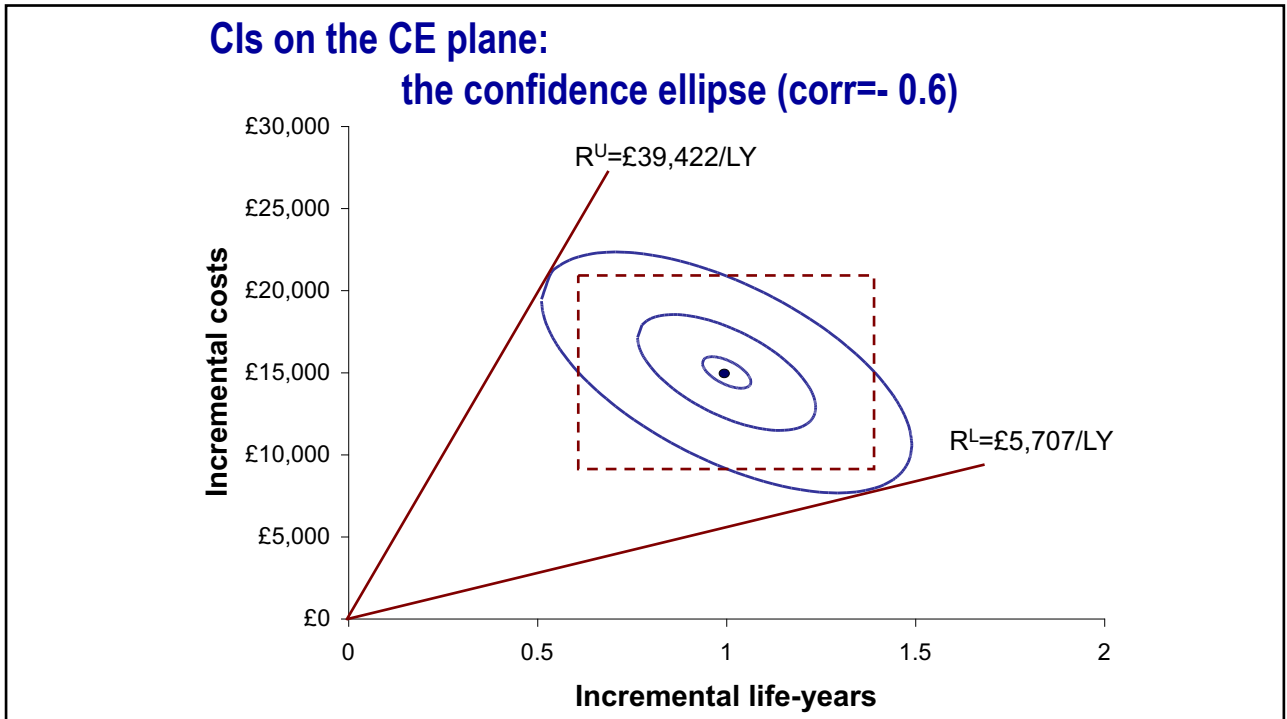
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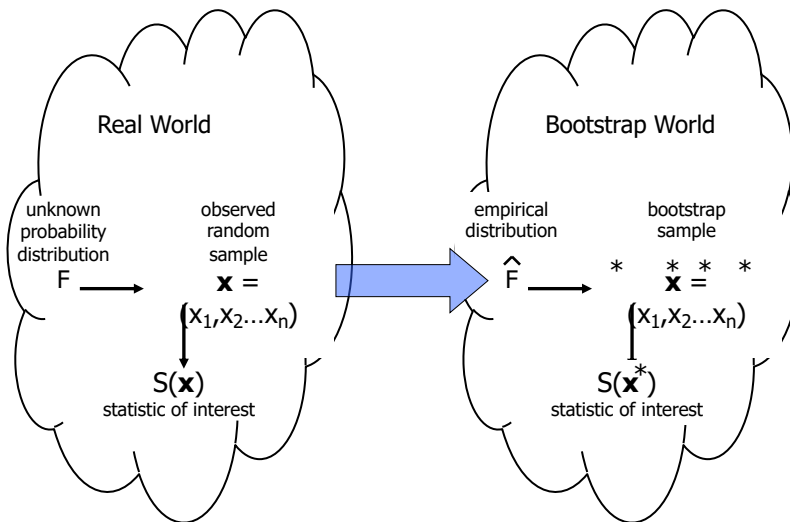


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## Two worlds: the real world and the bootstrap world



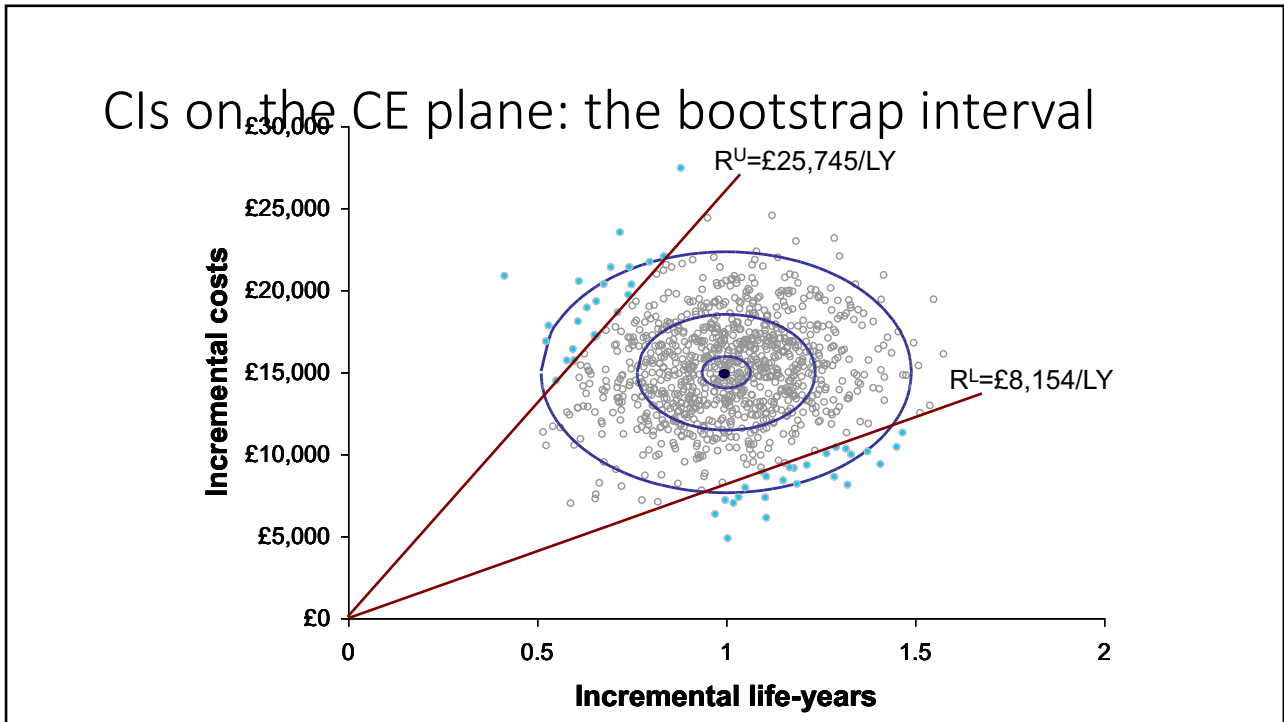
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## Bootstrapping the ICER

Four stage process:

1. Bootstrap  $n_c$  cost/effect pairs from the control group: calculate means
2. Bootstrap  $n_t$  cost/effect pairs from the treatment group: calculate means
3. Calculate the bootstrapped ICER from these bootstrapped means
4. Repeat many times to create the bootstrap estimate of the ICER sampling distribution

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### A parametric approach: Fieller's theorem

$\Delta\bar{C} - R\Delta\bar{E} \sim \text{Normally}$

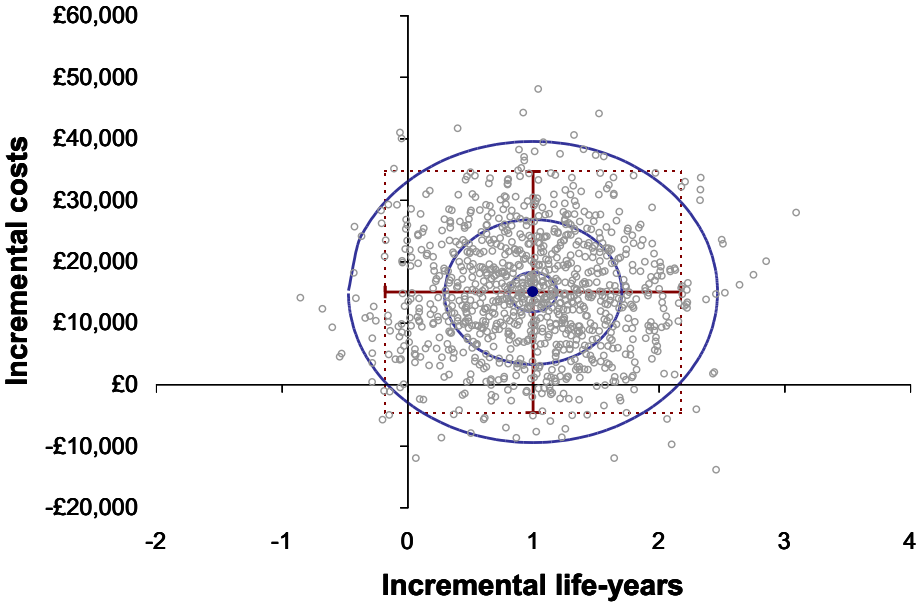
$\frac{\Delta\bar{C} - R\Delta\bar{E}}{\sqrt{\text{var}(\Delta\bar{C}) + R^2 \text{var}(\Delta\bar{E}) - 2R \text{cov}(\Delta\bar{C}, \Delta\bar{E})}} \sim N(0,1)$

$$\begin{aligned}
 & \left. \begin{aligned}
 & R^2 [\Delta E^2 - z_{\alpha/2}^2 \text{var}(\Delta E)] \\
 & - 2R [\Delta E \cdot \Delta C - z_{\alpha/2}^2 \text{cov}(\Delta E, \Delta C)] \\
 & + [\Delta C^2 - z_{\alpha/2}^2 \text{var}(\Delta C)] \\
 & = 0
 \end{aligned} \right\} \begin{array}{l} \text{Standard quadratic} \\ \text{equation in } R \end{array} \left\{ \begin{array}{l} aR^2 \\ +bR \\ +c \\ = 0 \end{array} \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{[\Delta E \cdot \Delta C - z_{\alpha/2}^2 \text{cov}(\Delta E, \Delta C)]}{\Delta E^2 - z_{\alpha/2}^2 \text{var}(\Delta E)} \\
 & \pm \frac{\sqrt{[\Delta E \cdot \Delta C - z_{\alpha/2}^2 \text{cov}(\Delta E, \Delta C)]^2 - [\Delta E^2 - z_{\alpha/2}^2 \text{var}(\Delta E)] \cdot [\Delta C^2 - z_{\alpha/2}^2 \text{var}(\Delta C)]}}{\Delta E^2 - z_{\alpha/2}^2 \text{var}(\Delta E)}
 \end{aligned}$$

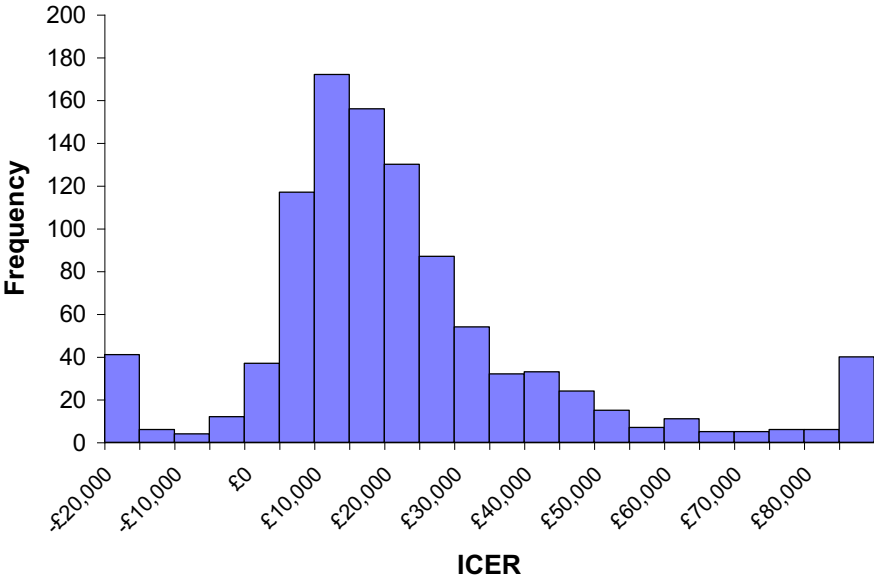
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### Non-significant differences?



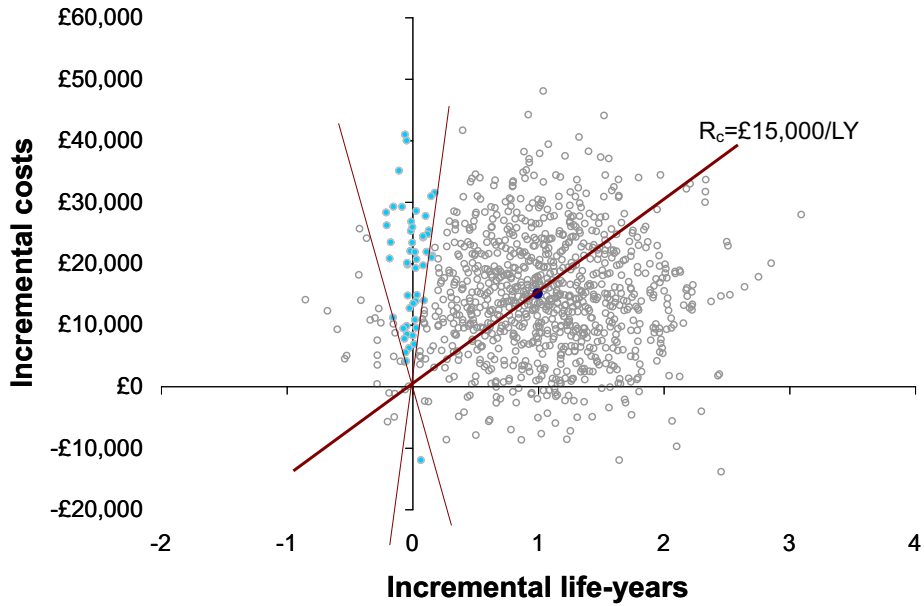
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### The estimated distribution of the ICER



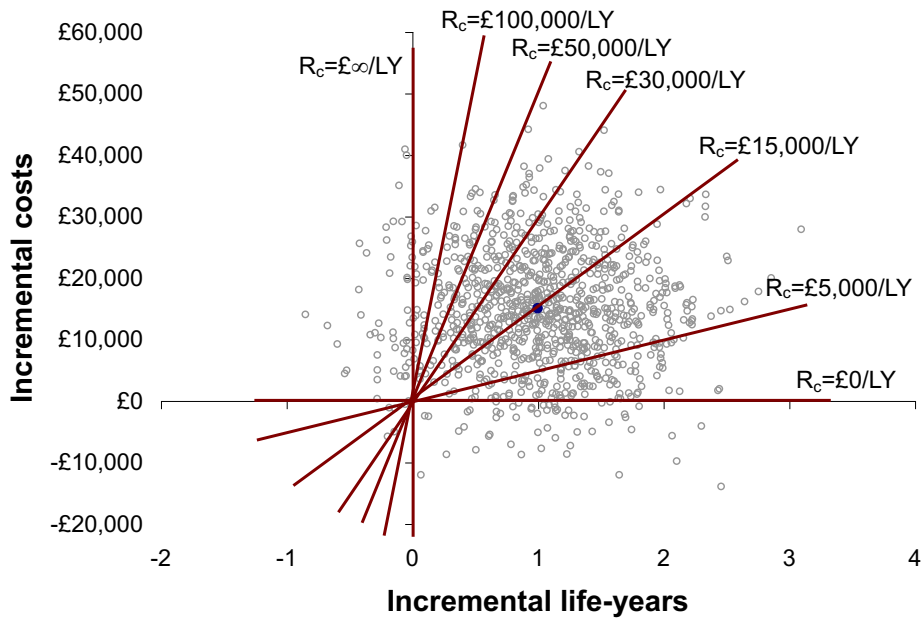
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### Problems with negative with negative ratios



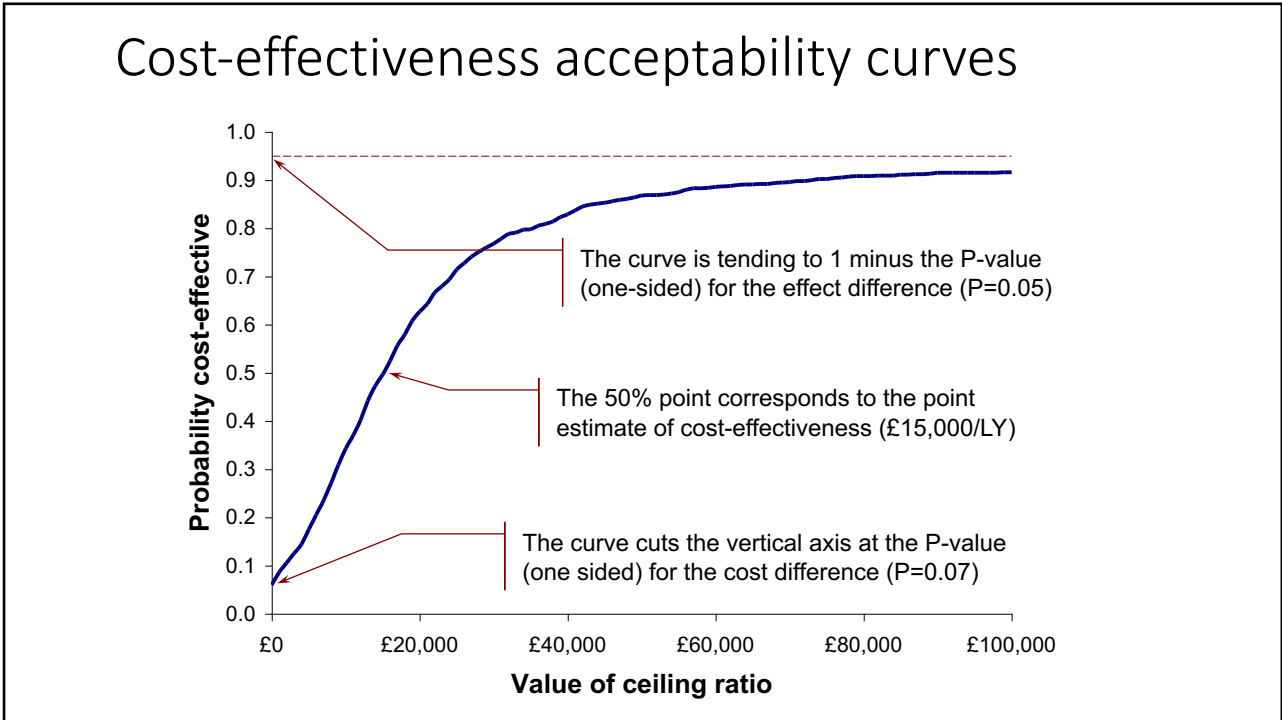
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### Uncertainty on the CE plane: using the decision rule

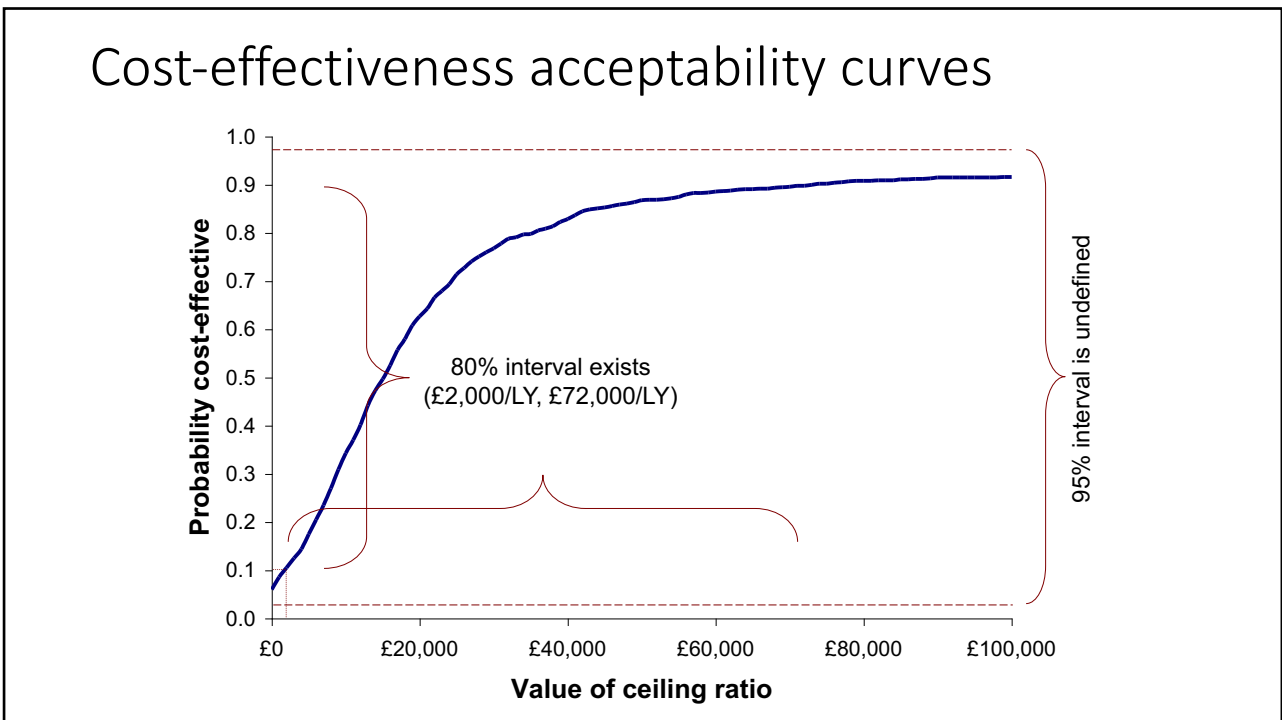


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## Trials versus models: false dichotomy?

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## Whither 'trial-based' analyses?

- Failure to compare all relevant options
- Truncated time horizon
- Lack of relevance to the decision context
- Failure to incorporate all evidence
- Inadequate quantification of uncertainty

*Source: Sculpher et al, 2006, Health Economics*

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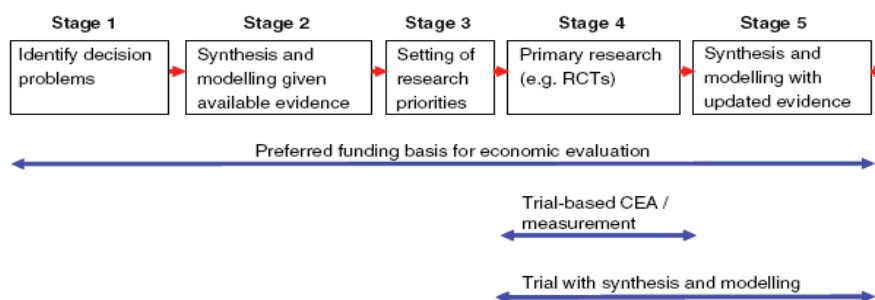
## Requirements of economic evaluation for decision making

- Clear statement and measurement of the objective function
- Consistent perspective
- Appropriate specification of the decision problem
- Appropriate time horizon
- All relevant evidence
- Relevant to the decision context
- Appropriate characterisation of uncertainty

*Source: Sculpher et al, 2006, Health Economics*

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## An iterative approach to economic appraisal



*Source: Sculpher et al, 2006, Health Economics*

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# UKPDS Outcomes Model v1

- Series of linked risk equations from UKPDS study
- Capable of predicting (quality adjusted) life expectancy and lifetime cost

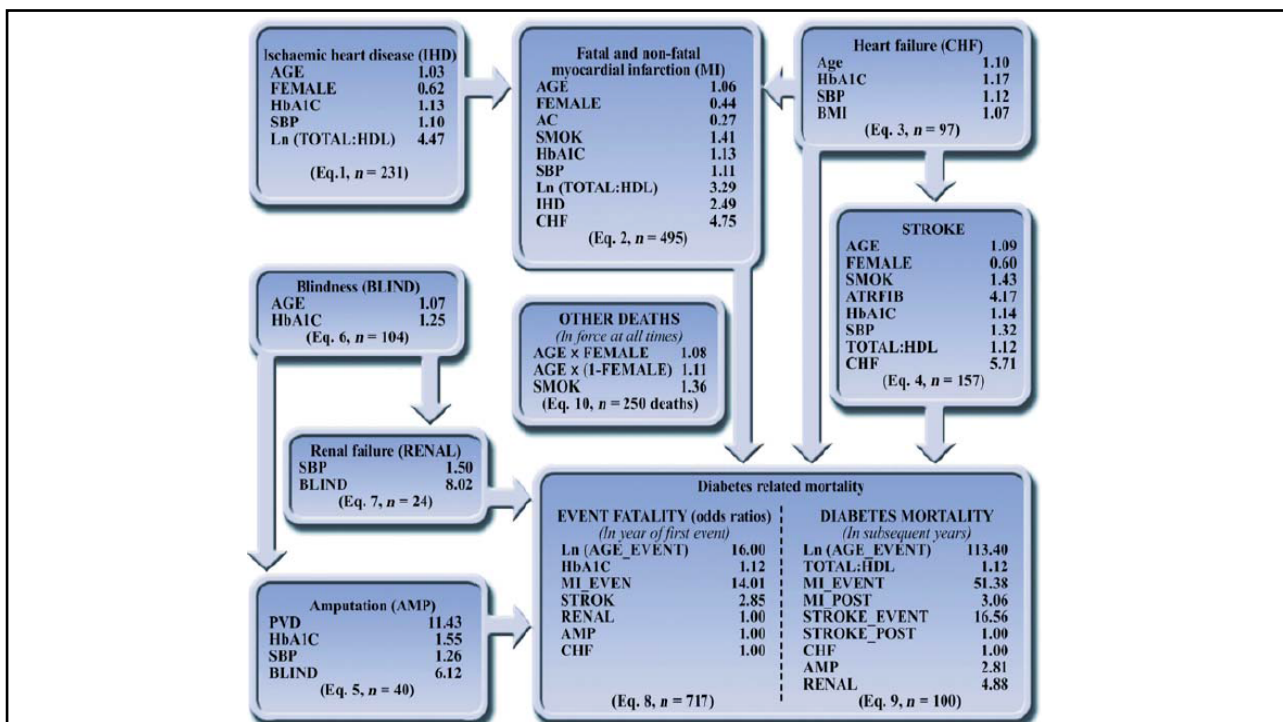
Diabetologia (2004) 47:1747–1759  
DOI 10.1007/s00125-004-1527-z

**Diabetologia**

## A model to estimate the lifetime health outcomes of patients with Type 2 diabetes: the United Kingdom Prospective Diabetes Study (UKPDS) Outcomes Model (UKPDS no. 68)

P. M. Clarke<sup>1, 4</sup> · A. M. Gray<sup>1</sup> · A. Briggs<sup>1</sup> · A. J. Farmer<sup>2</sup> · P. Fenn<sup>3</sup> · R. J. Stevens<sup>4</sup> · D. R. Matthews<sup>5</sup>  
I. M. Stratton<sup>4</sup> · R. R. Holman<sup>4</sup> · on behalf of the UK Prospective Diabetes Study (UKPDS) Group

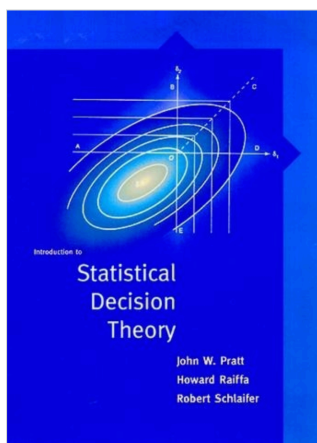
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# Statistical decision theory

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## Introduction to Statistical Decision Theory

By John Pratt, Howard Raiffa and Robert Schlaifer

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[Health Econ.](#) 1996 Nov-Dec;5(6):513-24.

### **An economic approach to clinical trial design and research priority-setting.**

Claxton K<sup>1</sup>, Posnett J.

#### **⊕ Author information**

#### **Abstract**

Whilst significant advances have been made in persuading clinical researchers of the value of conducting economic evaluation alongside clinical trials, a number of problems remain. The most fundamental is the fact that economic principles are almost entirely ignored in the traditional approach to trial design. For example, in the selection of an optimal sample size no consideration is given to the marginal costs or benefits of sample information. In the traditional approach this can lead to either unbounded or arbitrary sample sizes. This paper presents a decision-analytic approach to trial design which takes explicit account of the costs of sampling, the benefits of sample information and the decision rules of cost-effectiveness analysis. It also provides a consistent framework for setting priorities in research funding and establishes a set of screens (or hurdles) to evaluate the potential cost-effectiveness of research proposals. The framework permits research priority setting based explicitly on the budget constraint faced by clinical practitioners and on the information available prior to prospective research. It demonstrates the link between the value of clinical research and the budgetary restrictions on service provision, and it provides practical tools to establish the optimal allocation of resources between areas of clinical research or between service provision and research.

PMID: 9003938 DOI: [10.1002/\(SICI\)1099-1050\(199611\)5:6<513::AID-HEC237>3.0.CO;2-9](https://doi.org/10.1002/(SICI)1099-1050(199611)5:6<513::AID-HEC237>3.0.CO;2-9)

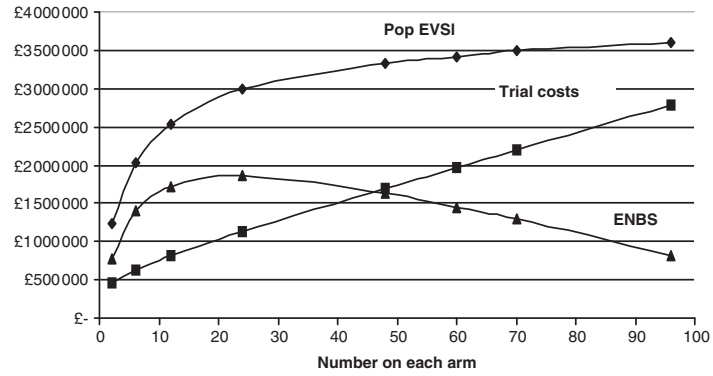
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## Expected Net Benefit of Sampling (ENBS)

- Is it cost-effective to run a new study? If so, to choose the best design (e.g. sample size per arm).
- Difference between monetarised gain from collecting further data from chosen study design, and the cost of that study
- $ENBS(n) = \text{population EVSI}(n) - \text{cost}(n)$

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Fig. 3. Population EVSI, trial costs and ENBS for the breast cancer screening example. Adapted from Ref. [12].



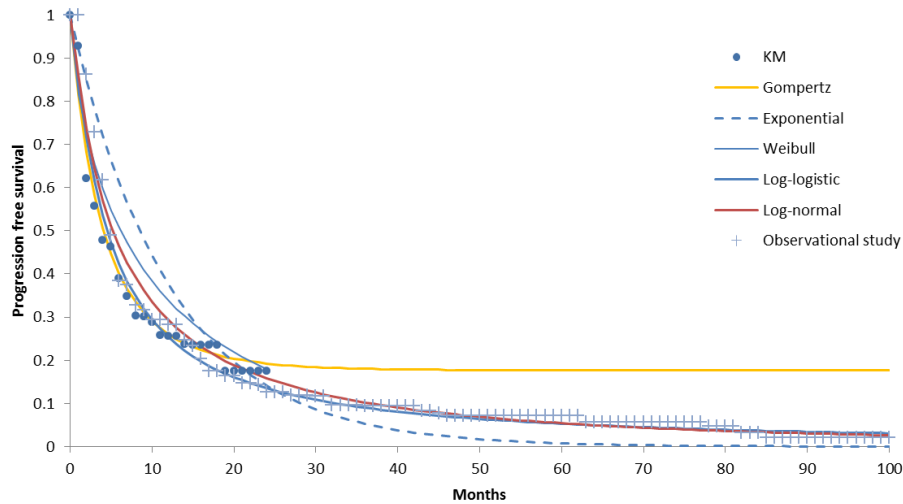
Welton et al. *Rheumatology* 2011;50:iv19-iv25

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# Survival analysis

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## Parametric survival - distribution selection



Coiffier (2012); Mak (2013)

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## Parametric PFS vs Kaplan-Meier - distribution selection (4)

- Latimer (2011) recommends selecting the most appropriate parametric model based on both within-trial fit, and external and clinical validity

Method	Description
<b>Within trial period</b>	
AIC & BIC statistics	Assess the relative fit of parametric models whilst accounting for the number of parameters
Cox-Snell residuals	Assess how closely a parametric function follows the Kaplan-Meier function
Cumulative hazard plot	Assess the behavior of the hazard function over time and the plausibility of the proportional hazards assumption
Log-cumulative hazard plot	Assess the behavior of the hazard function over time and the plausibility of the proportional hazards assumption
Quantile-quantile (Q-Q) plot	Assess how closely an accelerated-failure time treatment effect model fits the data
Visual inspection	Assess how closely a parametric function follows the Kaplan-Meier function and the clinical plausibility of the prediction in relation to other endpoints
<b>Extrapolation period</b>	
Monthly event probabilities	Compare event probabilities based on each parametric function and external longer term observational data
Visual inspection	Assess how closely the tail of a parametric function fitted to the active treatment arm(s) concur with external longer term observational Kaplan-Meier data

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## Cure modelling

- For some outcomes, a proportion of patients may never experience the event.
  - e.g. patients who are cured of their disease may never experience disease recurrence
- Identified graphically by a plateau in the Kaplan-Meier where the hazard equates to the general population hazard
- Standard parametric models may be incapable of fitting to these hazard functions
- May also be an interest in estimating the proportion of patient who are cured, referred to as the “cure fraction”

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## Parametric cure models

- Mixture cure models assume that a proportion of patients are cured and the excess (disease) hazard function tends to zero at the cure fraction.

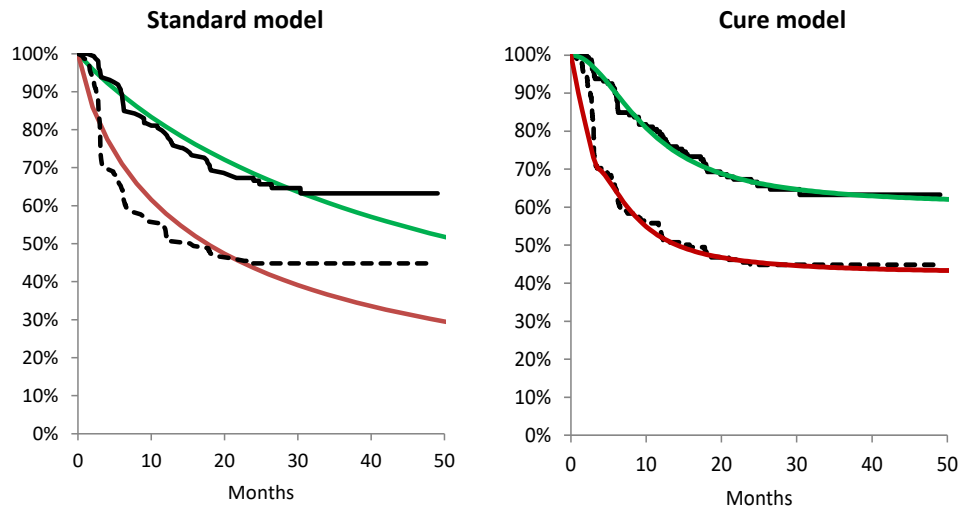
$$S(t) = S^*(t)[\pi + (1 - \pi)S(t_u)]$$

- $t$  is time
- $S^*(t)$  is the survival for the general population
- $\pi$  is the cure fraction
- $S(t_u)$  is the survivor function for uncured patients
- Need to choose a parametric form for  $S(t_u)$ 
  - Weibull, Lognormal, Generalised gamma
- Available using the `strsmix` command in Stata and other packages (SAS, R)

Lambert (2007)

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## Parametric cure models – application



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## Treatment switching

- Patients switch from control to treatment arm following primary endpoint
  - Common issue in oncology trials
- As a subset of patients in the control arm receive the benefit of treatment, overall survival times for patients who switched treatment are overestimated.
  - Failure to adjust for treatment crossover can result in an underestimated relative treatment effect.
  - Adjustment for treatment crossover aims to reduce bias in relative treatment effect estimates resulting from such treatment switching.
  - Methods that preserve randomisation are needed to provide unbiased treatment effect estimates in the presence of treatment switching

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## Methods for adjusting for treatment crossover

- NICE guidelines provide a range of approaches to consider when faced with treatment switching, including:
  - Rank Preserving Structural Failure Time Models (RPSFTM)
  - Iterative parameter estimation (IPE) algorithm
  - Inverse Probability of Censoring Weights (IPCW) method

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Comparative effectiveness

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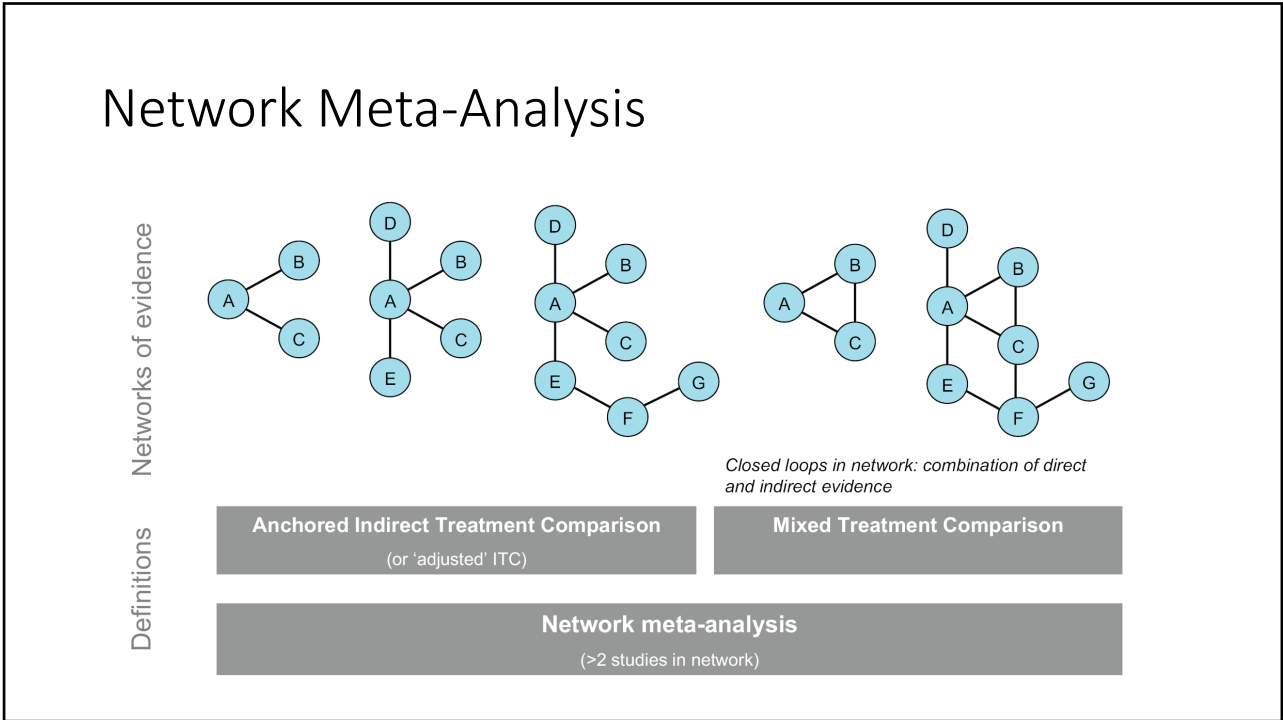
### The results of direct and indirect treatment comparisons in meta-analysis of randomized controlled trials

Heiner C. Bucher\*<sup>1</sup>, Gordon H. Guyatt, Lauren E. Griffith, Stephen D. Walter<sup>2</sup>  
Department of clinical epidemiology and biostatistics, McMaster university, Hamilton, Ontario, Canada, L8N 3Z5

PlumX Metrics

DOI: [https://doi.org/10.1016/S0895-4356\(97\)00049-8](https://doi.org/10.1016/S0895-4356(97)00049-8)

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General Medicine

## Network meta-analysis: the highest level of medical evidence?

Erlend G Faltinsen<sup>1</sup>, Ole Jakob Storebø<sup>1, 2</sup>, Janus C Jakobsen<sup>3, 4</sup>, Kim Boesen<sup>5</sup>, Theis Lange<sup>6, 7</sup>, Christian Gluud<sup>3</sup>

[Author affiliations +](#)

[View Full Text](#)  
<http://dx.doi.org/10.1136/bmjebm-2017-110887>

Statistics from Altmetric.com



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## Comparative effectiveness without a network?

Comparing existing but unconnected data:

- Naïve comparison
- Match adjusted indirect comparisons (MAIC)
- Simulated Trial Comparison (STC)

Single arm studies:

- Historical controls
- Synthetic controls
- Self control

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## Statistical methods for cost-effectiveness analysis: looking to the future

- Real world data, big data and personalised medicine
  - Application of ML and AI
  - Use of innovative methods for causal inference (MR / other IV approaches)
  - SEM (modelling components of CEA?)
- Refinement of existing methods
  - Methods for statistical estimation of counterfactuals
  - Application of existing VOI methods (under-used)
  - Novel survival analysis approaches (multi-state survival / competing risks)
  - Uncertainty in the face of multiple methods challenges (bootstrapping)